

Predicting Semantic Relations using Global Graph Properties

Yuval Pinter and Jacob Eisenstein

[@yuvalpi](https://twitter.com/yuvalpi)

[@jacobeisenstein](https://twitter.com/jacobeisenstein)

code: github.com/yuvalpinter/m3gm

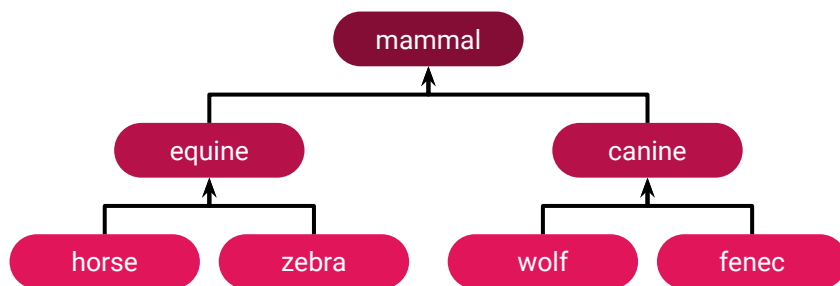
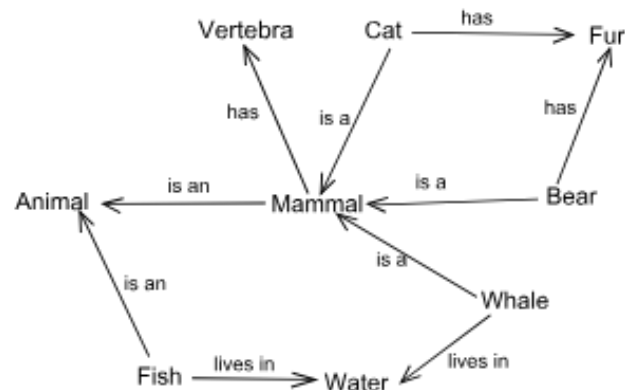
contact: uvp@gatech.edu



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of **Tech**nology®

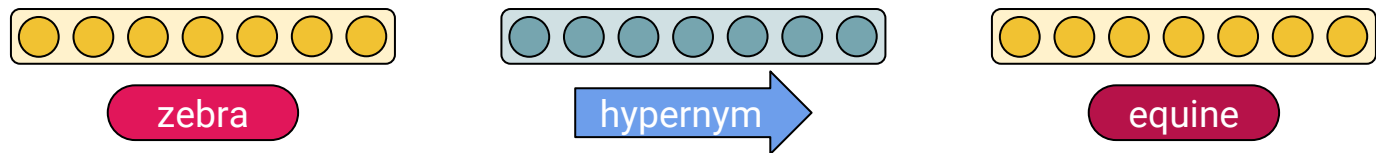
Semantic Graphs

- **WordNet**-like resources are curated to describe relations between word senses
- The graph is **directed**
 - Edges have form $\langle S, r, T \rangle$: $\langle \text{zebra}, \text{is-a}, \text{equine} \rangle$
 - Still, some relations are symmetric
- Relation types include:
 - Hypernym (is-a) $\langle \text{zebra}, r, \text{equine} \rangle$
 - Meronymy (is-part-of) $\langle \text{tree}, r, \text{forest} \rangle$
 - Is-instance-of $\langle \text{rome}, r, \text{capital} \rangle$
 - Derivational Relatedness $\langle \text{nice}, r, \text{nicely} \rangle$



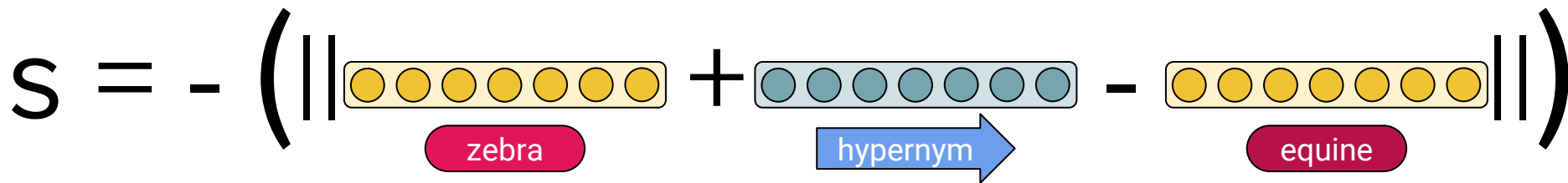
Semantic Graphs - Relation Prediction

- The task of predicting relations (*zebra* is a <BLANK>)
- **Local** models use embeddings-based composition for scoring edges



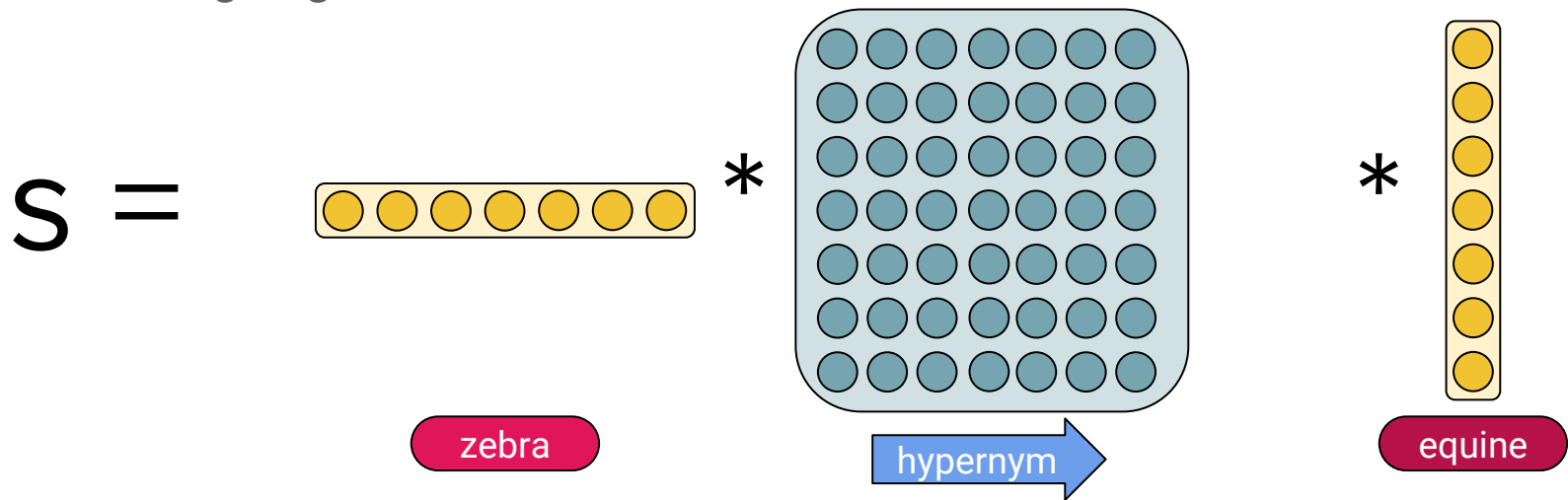
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$$S = - \left(\left\| \left[\text{zebra} \right] + \left[\text{hypernym} \right] - \left[\text{equine} \right] \right\| \right)$$


Semantic Graphs - Relation Prediction

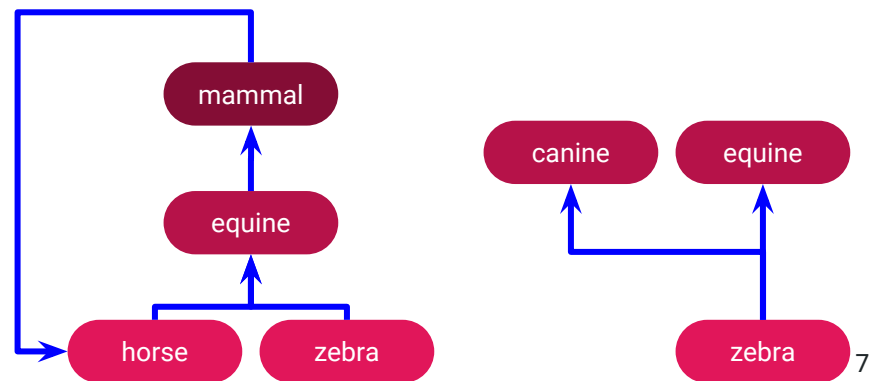
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Full-Bilinear (Bilin) [Nickel et al. 2011]

Semantic Graphs - Relation Prediction

- The task of predicting relations (*zebra* is a *<BLANK>*)
- **Local** models use embeddings-based composition for scoring edges
- Problem: task-driven method can learn unreasonable graphs



Incorporating a Global View

- We want to avoid unreasonable graphs
- Imposing hard constraints isn't flexible enough
 - Only takes care of **impossible graphs**
 - Requires domain knowledge
- We still want the local signal to matter - it's very strong.

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- We still want the local signal to matter - it's very strong.
- Our solution: an additive, learnable **global graph score**

Score(<*zebra*, hypernym, *equine*> | **WordNet**) =

$$s_{\text{local}}(\text{edge}) + \Delta(s_{\text{global}}(\text{WN} + \text{edge}), s_{\text{global}}(\text{WN}))$$

Global Graph Score

- Based on a framework called Exponential Random Graph Model (**ERGM**)
- The score $s_{\text{global}}(\mathbf{WN})$ is derived from a log-linear distribution across possible graphs that have a fixed number n of nodes

$$p_{\text{ERGM}}(\mathbf{WN}) \propto \exp(\boldsymbol{\theta}^T \cdot \Phi(\mathbf{WN}))$$

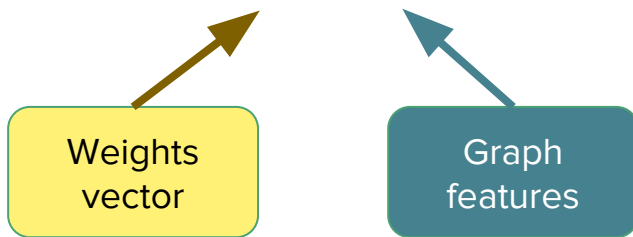
Weights vector

Graph features

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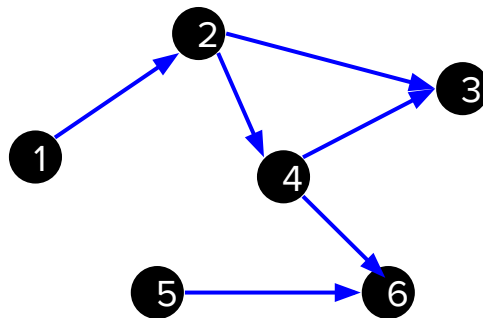
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- OK. What are the **features**?

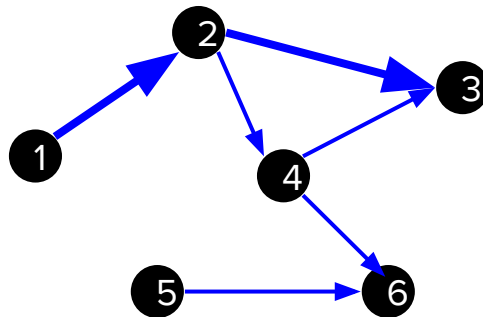
Graph Features (*Motifs*)

- #edges: 6
- #targets: 4
- #3-cycles: 0
- #2-paths: 4
- Transitivity: $\frac{1}{4} = 0.25$



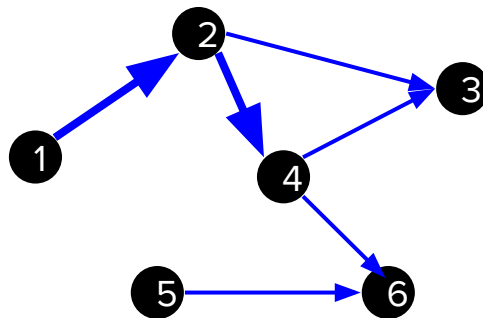
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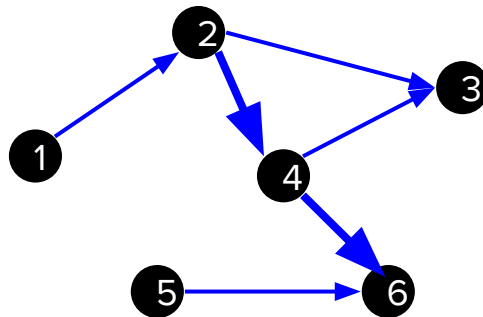
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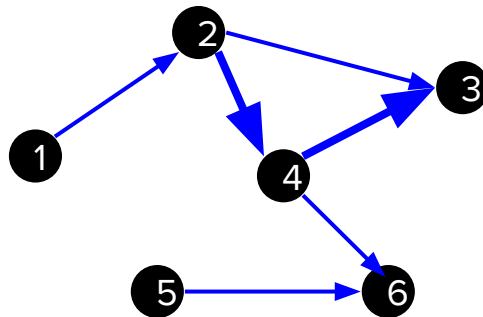
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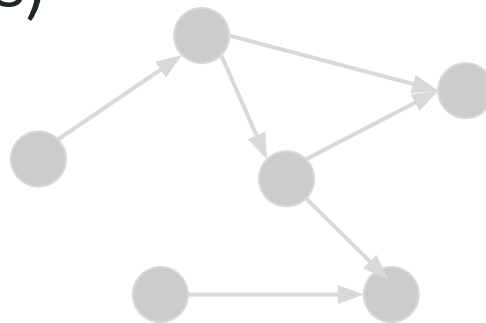
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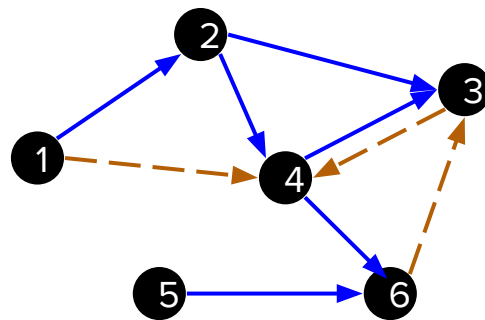
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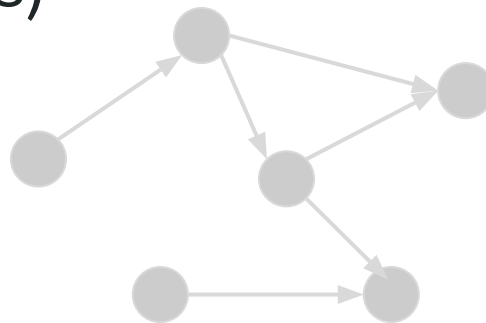
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- Transitivity (b-o-b): $\frac{2}{3} = 0.67$



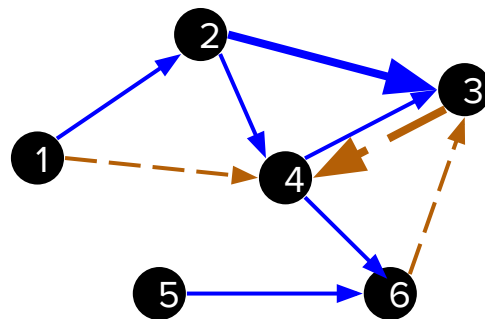
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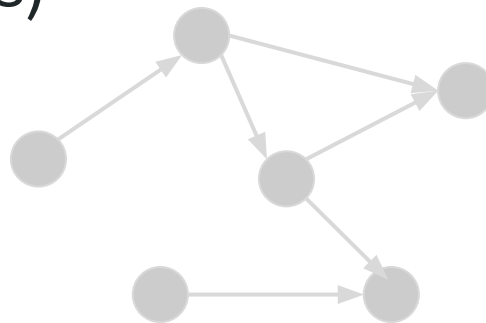
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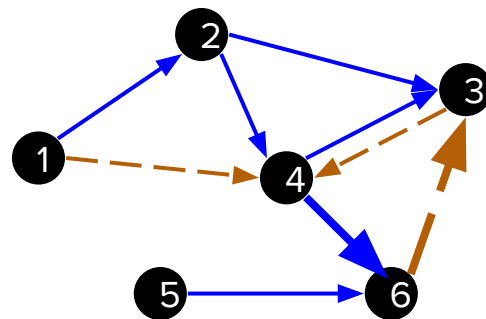
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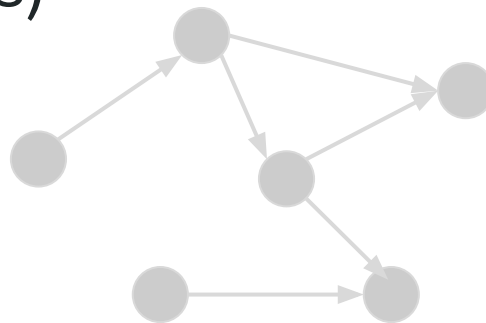
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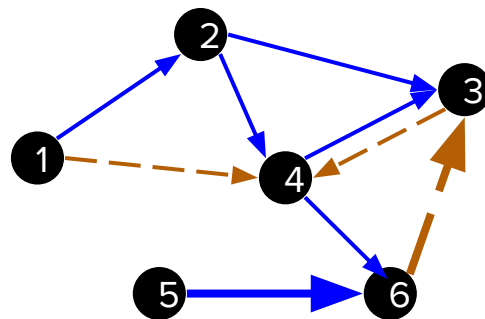
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ERGM Training

- Estimating the scores for all possible graphs to obtain a probability distribution is **implausible**
 - Number of possible directed graphs with n nodes: $O(\exp(n^2))$
 - n nodes, R relations: $O(\exp(R*n^2))$
 - Estimation begins to be hard at $\sim n=100$ for $R=1$. In WordNet: $n = 40K$, $R = 11$.

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What can we do?

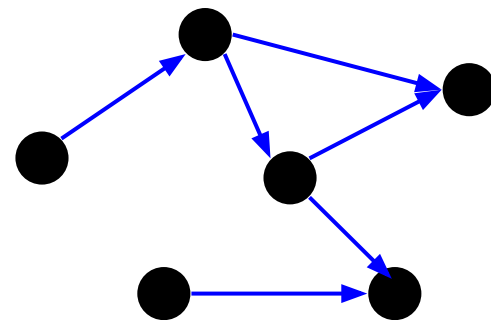
- Decompose score over dyads (node pairs) in graph
- Draw and score negative sample graphs

Max-Margin Markov Graph Model (M3GM)

- Sample negative graphs from the “local neighborhood” of the true WN

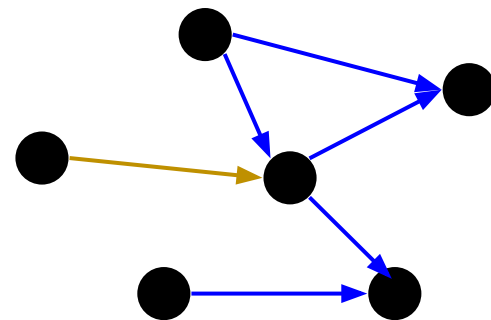
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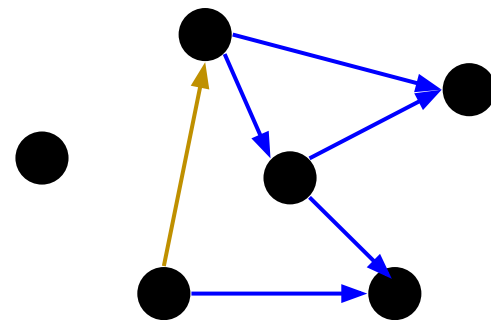
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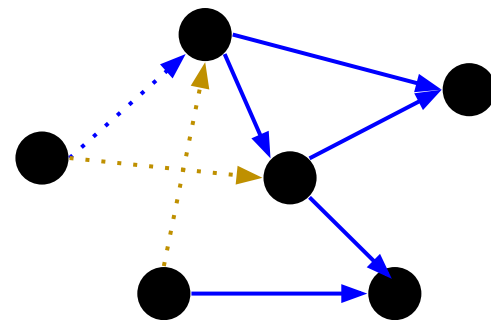
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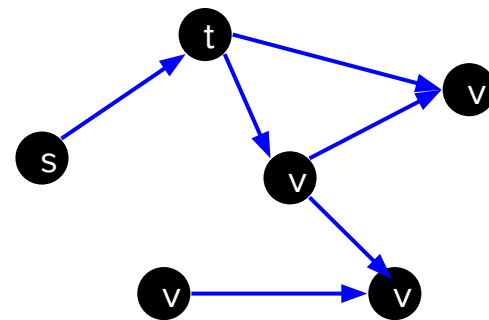
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- Loss = $\text{Max} \{0, 1 + \text{score}(\text{negative sample}) - \text{score}(\text{WN})\}$



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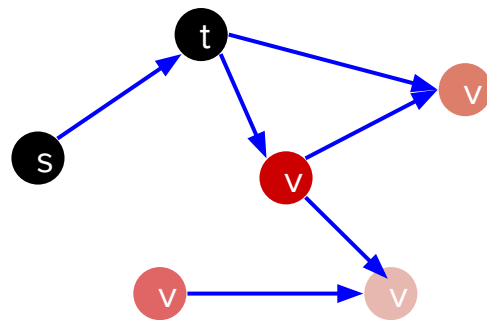
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Max-Margin Markov Graph Model (M3GM)

- It's important to choose an appropriate **proposal distribution** (source of the negative samples)
- We want to make things **hard** for the scorer

$$Q(v|s, r) \propto s_{\text{local}}(\langle s, r, v \rangle)$$



Evaluation

- Dataset - WN18RR
 - No reciprocal relations (hypernym \Leftrightarrow hyponym)
 - **Still includes symmetric relations**
- Metrics - MRR, H@10

- Rule baseline - take symmetric if exists in train
 - Used in all models as default for symmetric relations
- Local models
 - Synset embeddings - averaged from FastText
- M3GM (re-rank top 100 from local)
 - \sim 3000 motifs, \sim 900 non-zero

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transE

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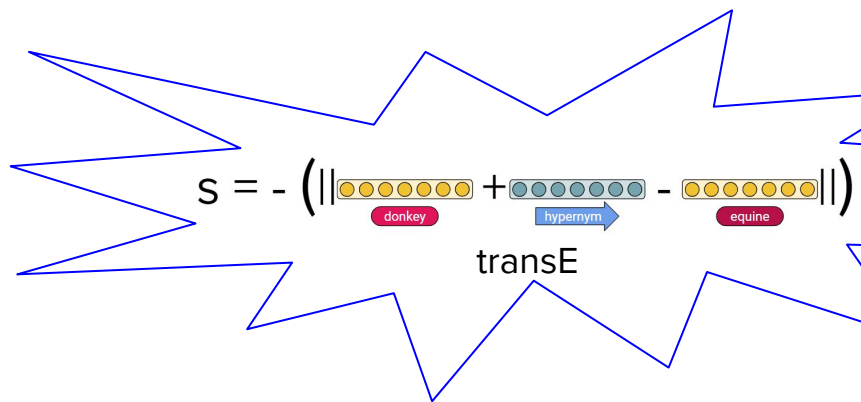
DistMult

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Bilin

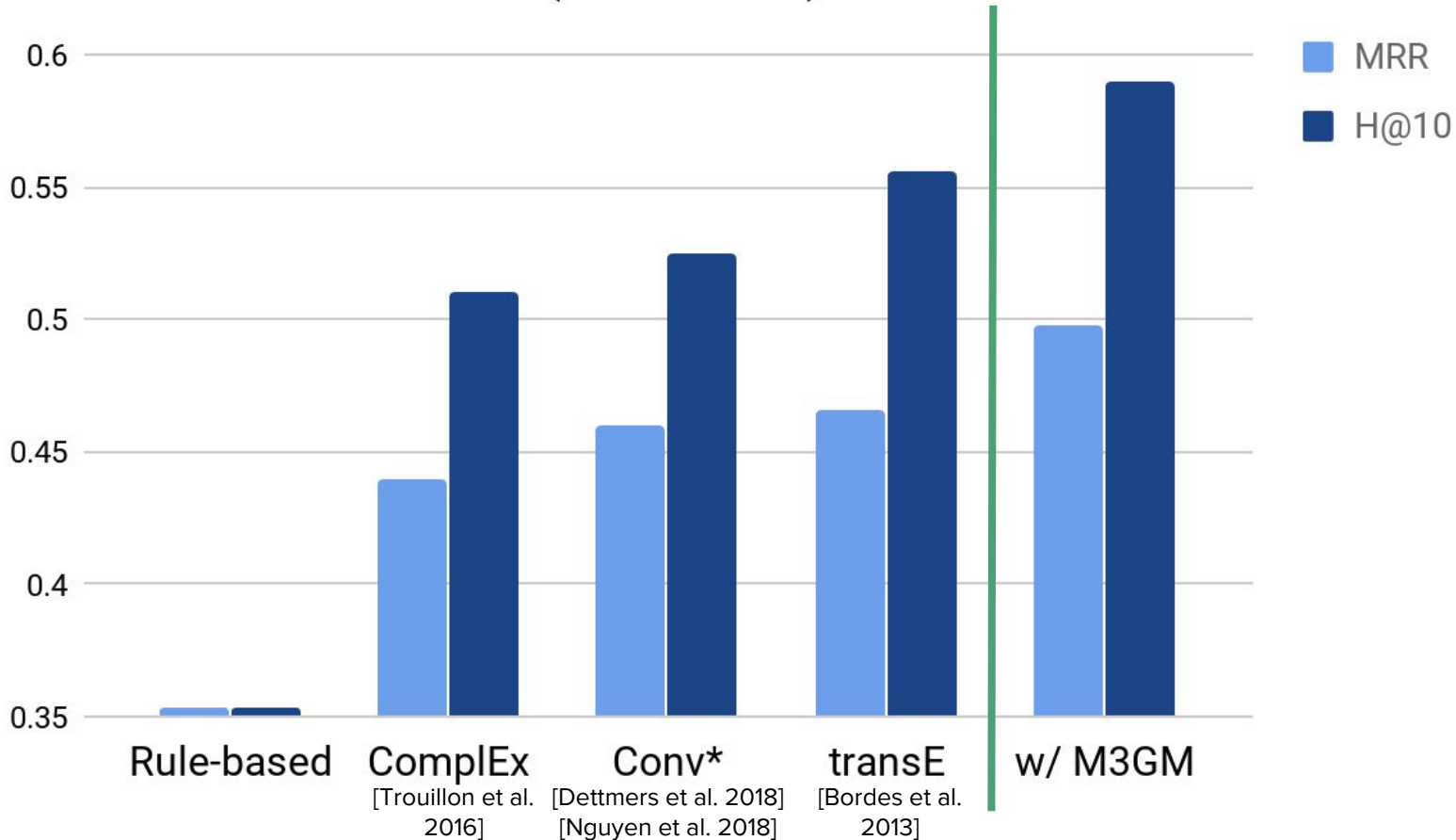
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Relation Prediction (WN18RR)

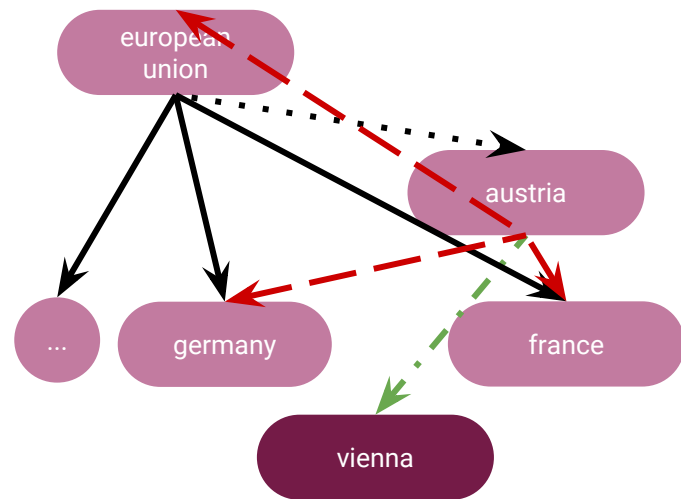
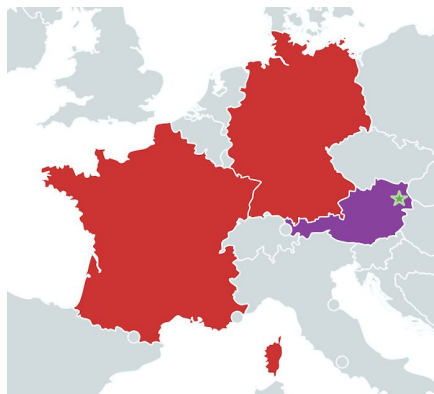


Feature Analysis

- Motifs with heavy positive weights:
 - Targets of *has_part*
 - Two-paths *hypernym* → *derivationally_related_form*
- Motifs with heavy negative weights:
 - Targets of *hypernym*
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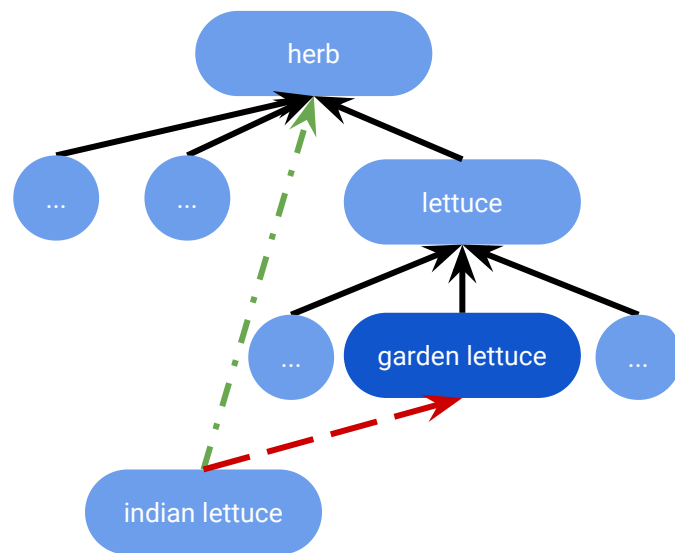
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- Seen in training data
- - - → Local-only prediction
- · - · → M3GM prediction
- · · · → Unseen in data

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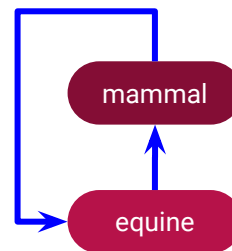
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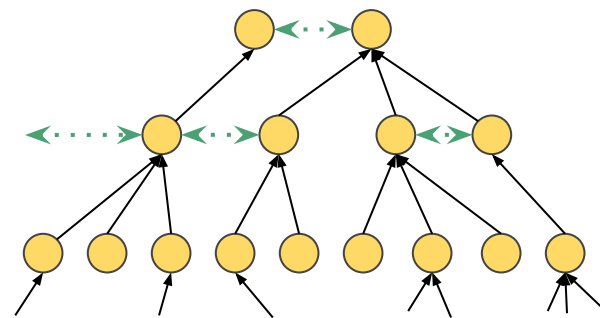


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“Derivations occur in the abstract parts of the graph”

(*bodega / canteen vs. shop*)



→ Hyponym

↔ Deriv. Related form

Feature Analysis

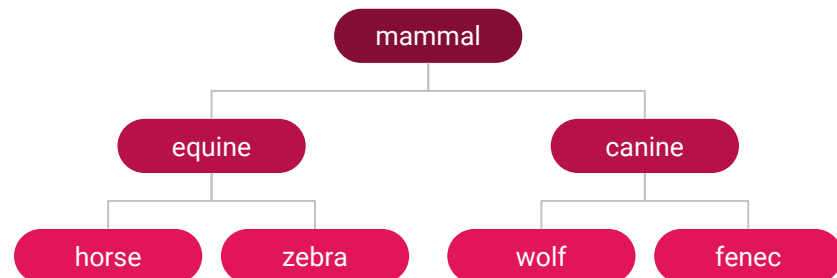
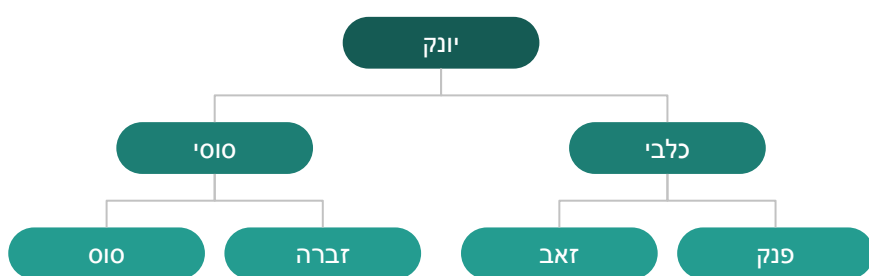
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Nouns

Verbs

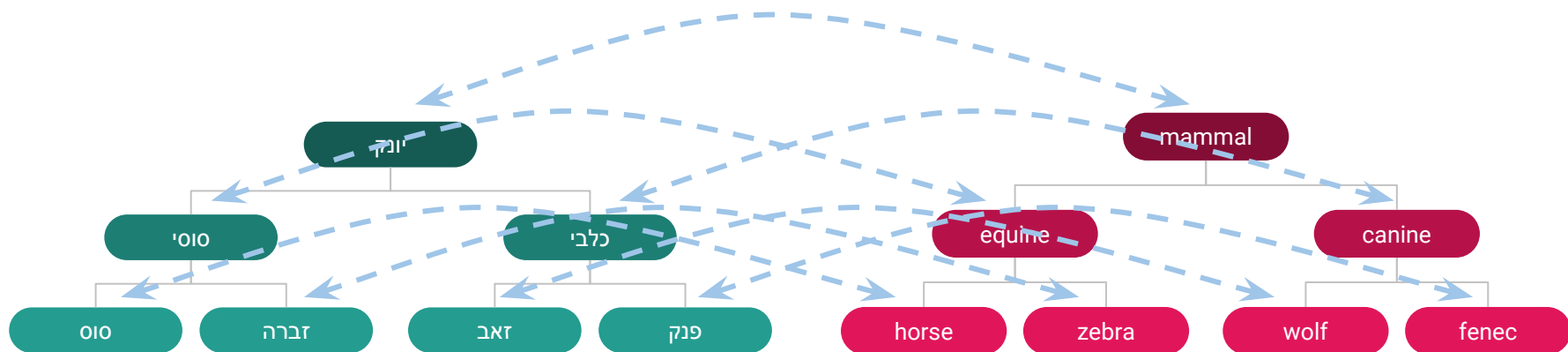
Future Work

- Multilingual transfers of semantic graphs



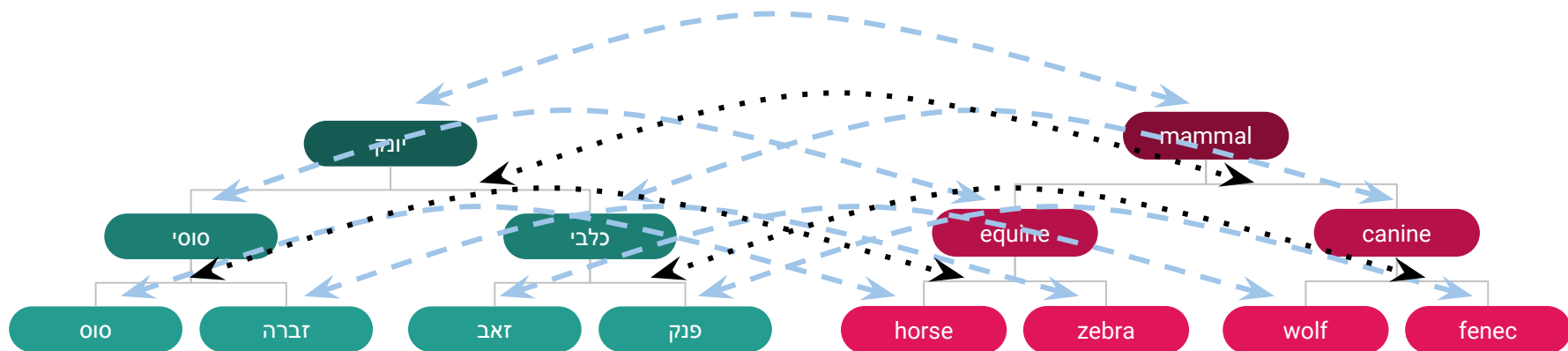
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- Can we introduce global features to help?



Conclusion

- Global reasoning of graph features is beneficial for relation prediction
- Works well on top of strong local models
- Applicable to large graphs with dozens of relation types ← **M3GM**
- Orthogonal of word / synset embedding techniques
- Finds a wide variety of linguistic patterns in semantic graphs

Thanks

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- YOU!



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