

17/11/16

Assignment 1 in  
Date: Alg's (Due to Dec. 10)

- 1) Describe an alg' that colors an oriented tree in  $O(\log^{(n)} n)$  colors. Analyze it, it's recursive.
- 2) Analyze the recursive formula that governs the running time of Cole-Vishkin's alg' for an oriented tree.  
The same as  $\sqrt{\text{problem}}$ , best for the version of Cole-Vishkin for  $n$ -vx graphs with maximum degree at most  $\Delta$ .
- 4) We are given an  $\alpha$ -coloring  $\phi$  of an oriented tree. Using just one single application of the Shift-Down procedure and without using Cole-Vishkin's

recoloring routine,  
color the tree into 5 colors  
properly, w/ as few recolors as  
possible.

5) Devise an alg' that  
computes the diameter of an  
oriented, possibly wtd tree, in  
CONGEST model, in  $O(D)$  time.  
Prove correctness.

6) Show that Maximal Matching  
(under containment) is at least a  
2-approximation of Maximum  
Cardinality Matching.

7) Prove Easy! that the  
chromatic number of

Brooks's graph is 4.  
Try to think about a triangula-  
-free graph with chromatic  
number 5.

Enjoy!