

# Unique Permutation Hashing, Experiment Results

by

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# UNIQUE PERMUTATION

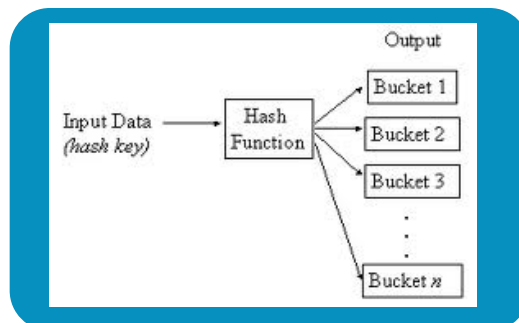
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# REPORT

# Table of Contents



INTRODUCTION	3
• Performance analysis of hashing computations	
SUMMARY	16
BIBLIOGRAPGHY	17

## Introduction:

The Unique Permutation hash function, an ingenious proposition by Prof. Shlomi Dolev, offers superior and preferable data structure hashing implementations of applications that support dictionary operations of *inserting*, *searching* & *deleting*. It does so in comparison to other hashing functions such as linear probing, quadratic probing and doubling hashing (currently one of the preeminent methods available for open addressing).

## Performance analysis of hashing computations:

Below is code (written in the python language) that implements the newly proposed Unique Permutation Hashing and provides a performance scheme of its hashing properties in comparison to linear probing, quadratic probing and double hashing.

```

from random import *

def factorial(x):
    if x == 1:
        return 1
    else:
        return x * factorial(x-1)

Tests = input('How many tests do you want to run?')
tableSize = input('Please state the size of the table you would wish to have...')
                # preferably should be prime
r = factorial(tableSize) # This reduces the probability for key duplication
Table = [False] * tableSize
empty = False

```

```

probes = 0
loadFactor = input('Choose your preferred loadFactor...')
    # (Numbers of Keys / Table slots)
print '\n'
knum = int(loadFactor*tableSize) # Number of keys based on load factor

# Generates a set of random keys to be hashed into the table
def setOfKeys():
    lists = []
    i = 0
    while i < knum:
        lists.append(randint(0,r-1))
        i += 1
    return lists

def numberOfTests():
    keys_list = []
    for i in range(Tests):
        keys_list += [setOfKeys()]
    return keys_list

key_sets = numberOfTests()

def linearProbe(key):
    global probes
    h = ( key % tableSize)
    for i in range(len(Table)):
        hi = ( (h + i) % len(Table) )
        if Table[hi] == empty:
            Table[hi] = key
            return
    else:
        probes += 1 # Number of probes made

```

```

def quadHashing(key):
    global probes
    h = (key % tableSize)
    for i in range(tableSize):
        h1 = ((h + i + 3*(i**2)) % tableSize)
        if Table[h1] == empty:
            Table[h1] = key
            return
    else:
        probes += 1 # Number of probes made

```

```

def doubleHashing(key):
    global probes
    h = (key % tableSize)
    h1 = 1 + (key % (tableSize-1))
    for i in range(tableSize):
        h2 = (h + (i * h1)) % tableSize
        if Table[h2] == empty:
            Table[h2] = key
            return
    else:
        probes += 1 # Number of probes made

```

```

def variance(listOfValues,mean):
    variance = 0
    for i in listOfValues:
        variance = variance + (i - mean)**2
    variance = float(variance) / (len(listOfValues))
    return variance

```

```

def perm(N): # Generates permutations and helps with visual puporses
    table_size = len(N) # to ensure that permutations generated in Unique

```

```

if table_size <= 1: # are indeed correct
    return [N]
return [p[:i]+[N[0]]+p[i:] for i in xrange(table_size) for p in perm(N[1:])]

def permutations(n):
    permutations = perm(range(1,n+1))
    return permutations

def convert(probe,seq): # finds next probe number not taken in the probe_seq
    seq = sorted(seq)
    index = 0
    if seq == []:
        return probe
    while index < len(seq) and seq[index] <= probe:
        probe += 1
        index += 1
    return probe

class Initialize:
    def __init__(self,i,key,probe_seq): # Gets input of the
        self.tableSize = tableSize # necessary data
        self.i = i # tracks the number of probes already made
        self.Kprime = key
        self.probe_seq = probe_seq
        self.M = factorial(tableSize)
        self.key = key

    def __str__(self): # Prints the Permutation Object created
        return 'Number of slots in the table = ' + str(self.tableSize) + '\n' \
            'Probe counter(tracks # of probes made) at initial state = ' + str(self.i) \
            + '\n' \
            'Probe sequence = ' + str(self.probe_seq) + '\n' \

```

```

' Key to be hashed =' + str(self.key) + '\n' \
' M (N-1-i) = ' + str(self.M)

def get(self):
    return self.i, self.Kprime, self.probe_seq

def computation(self): # Finds the kth permutation
    if (self.tableSize - self.i) == 0:
        return
    M = self.M / (self.tableSize - self.i)
    probe = (self.Kprime / M) + 1 # Probes
    k = self.Kprime % M # indicates probed numbers so far
    next_probe = convert(probe, self.probe_seq)
    self.probe_seq.append(next_probe)
    self.i += 1 # Keeps track of the probes already made
    self.M = M
    self.Kprime = k
    if len(self.probe_seq) == self.tableSize:
        return next_probe
    return next_probe

def Hash(self, key): # Uniquely Inserts a key to its appropriate slot
    global probes # in the table
    full = (empty not in Table)
    if full:
        print 'Table Overload: The table is FULL'
        return
    index = self.computation()
    if index is None: # Error in Inserting Key
        return
    if Table[index - 1] == empty:
        Table[index - 1] = key
    else:

```



```

        self.Hash(key)
        probes += 1

def create(): # Creates a list of objects
    MasterList = []
    Objects = [] # list of objects created. Important for visual reasons only
    j = 0
    while j < len(key_sets):
        ListWithinList = []
        for key in key_sets[j]:
            ListWithinList.append(Initialize(o,key,[]))
        MasterList.append(ListWithinList)
        j += 1
    return MasterList

#Prints the Physical Representation of the objects created.
#Code is however skipped as its only vital for visual purposes
for lists in MasterList:
    list1 = []
    for objects in lists:
        list1.append(objects.get())
    Objects.append(list1)
print Objects

def genericTest(name,func = None):
    global Table
    global probes
    j = 0
    probeRecord = []
    keyObjects = create()
    while j < len(key_sets):
        Table = [False] * tableSize # Empties table before beginning new test
        probes = 0

```

```

if name != 'UNIQUE HASHING TEST':
    for key in key_sets[j]: # Iterates through keys in each list of keys
        func(key)
        #print probes
        #print Table ### uncommment to print the various individual tables
    probeRecord.append(probes)
else:
    for objects in keyObjects[j]:
        objects.Hash(objects.key)
        # print probes
    probeRecord.append(probes)
j += 1

```

```

mean = float(sum(probeRecord)) / len(key_sets)
var = variance(probeRecord,mean)
stddev = var**(0.5)

```

```

print name
print '-----'
print 'Table slots = ',tableSize
print 'Load factor(# keys/#table entries) = ',loadFactor
print 'Number of keys = ',knum
print 'Number of tests conducted = ',len(key_sets)
print 'Total Number of probes = ', sum(probeRecord)
print 'Average number of probes = ', mean
print 'Variance(Probes) = ',var
print 'Standard Deviation of probes = ',stddev

```

```

def test1():
    genericTest('LINEAR PROBING TEST',linearProbe)

```

```

def test2():
    genericTest('QUADRATIC PROBING TEST',quadHashing)

```

```
def test3():
    genericTest('DOUBLE HASHING TEST',doubleHashing)
```

```
def test4():
    genericTest('UNIQUE HASHING TEST')
```

```
#####
```

```
# TEST PANEL#    #
```

```
def masterTests(): #
```

```
    test1()    #
```

```
    print '\n'    #
```

```
    test2()    #
```

```
    print '\n'    #
```

```
    test3()    #
```

```
    print '\n'    #
```

```
    test4()    #
```

```
#####
```

```
masterTests()
```

Upon Running the above code, one gets statistics on the number of probes made for each hashing technique. The tests are run using the same set of keys. The large number of tests is to ensure that the

## LINEAR PROBING TEST

---

Table slots = 97

Load factor(# keys/#table entries) = 1

Number of keys = 97

Number of tests conducted = 1000

Total Number of probes = 533844

Average number of probes = 533.844

Variance(Probes) = 22788.641664  
 Standard Deviation of probes = 150.959072811

### QUADRATIC PROBING TEST

---

Table slots = 97  
 Load factor(# keys/#table entries) = 1  
 Number of keys = 97  
 Number of tests conducted = 1000  
 Total Number of probes = 395047  
 Average number of probes = 395.047  
 Variance(Probes) = 5674.056791  
 Standard Deviation of probes = 75.3263353084

### DOUBLE HASHING TEST

---

Table slots = 97  
 Load factor(# keys/#table entries) = 1  
 Number of keys = 97  
 Number of tests conducted = 1000  
 Total Number of probes = 311074  
 Average number of probes = 311.074  
 Variance(Probes) = 3116.102524  
 Standard Deviation of probes = 55.8220612661

### UNIQUE HASHING TEST

---

Table slots = 97  
 Load factor(# keys/#table entries) = 1

Number of keys = 97

Number of tests conducted = 1000

Total Number of probes = 308883

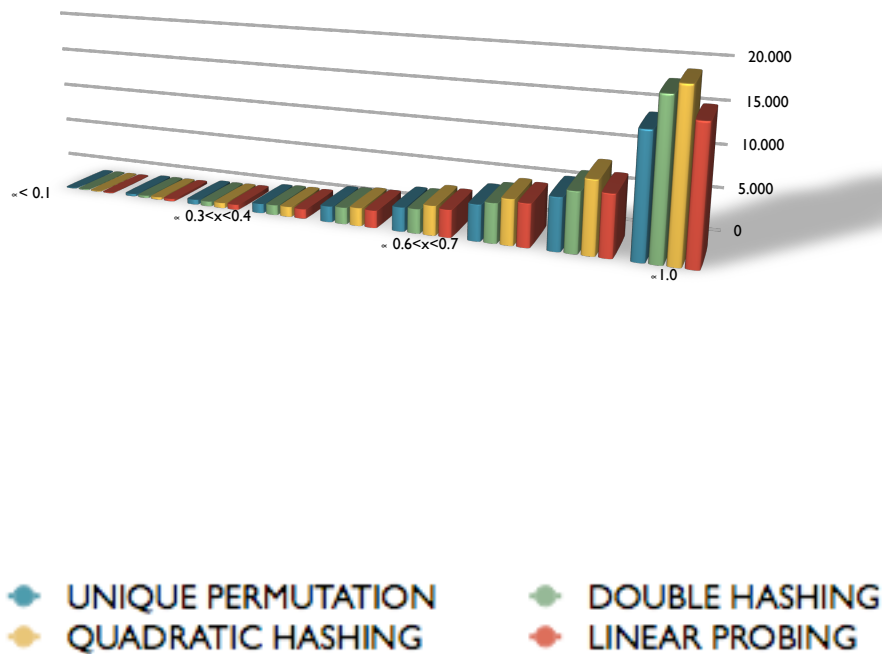
Average number of probes = 308.883

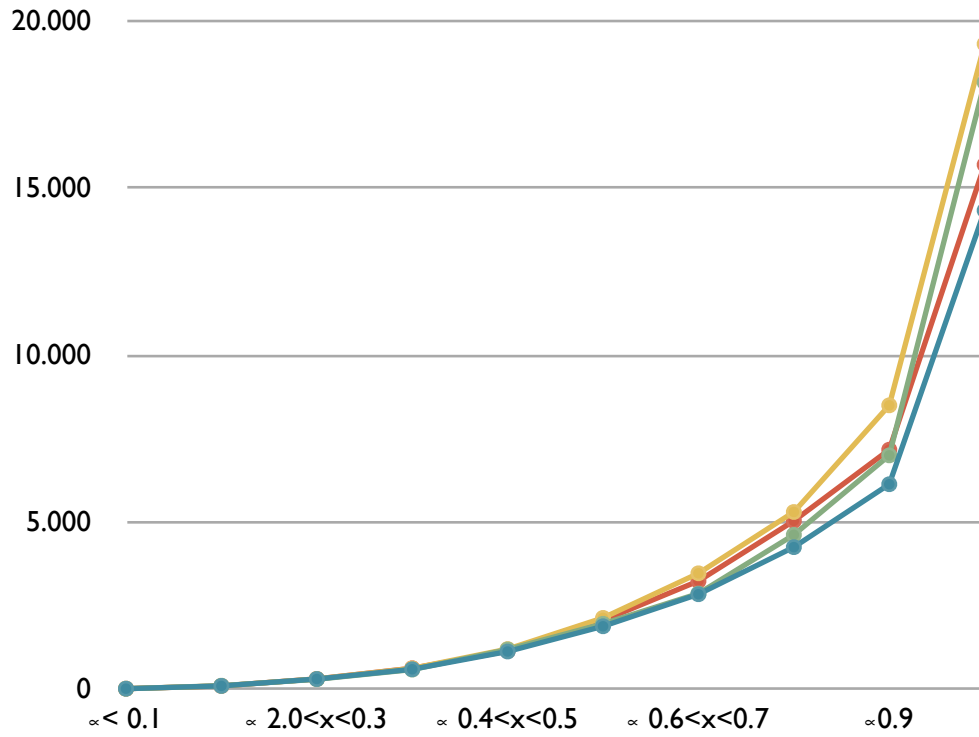
Variance(Probes) = 2740.773311

Standard Deviation of probes = 52.3523954657

The snippet above clearly shows the efficiency of the Unique Permutation Hash function.

Below are statistics and graphical representations of tests run with table size(n) = 11



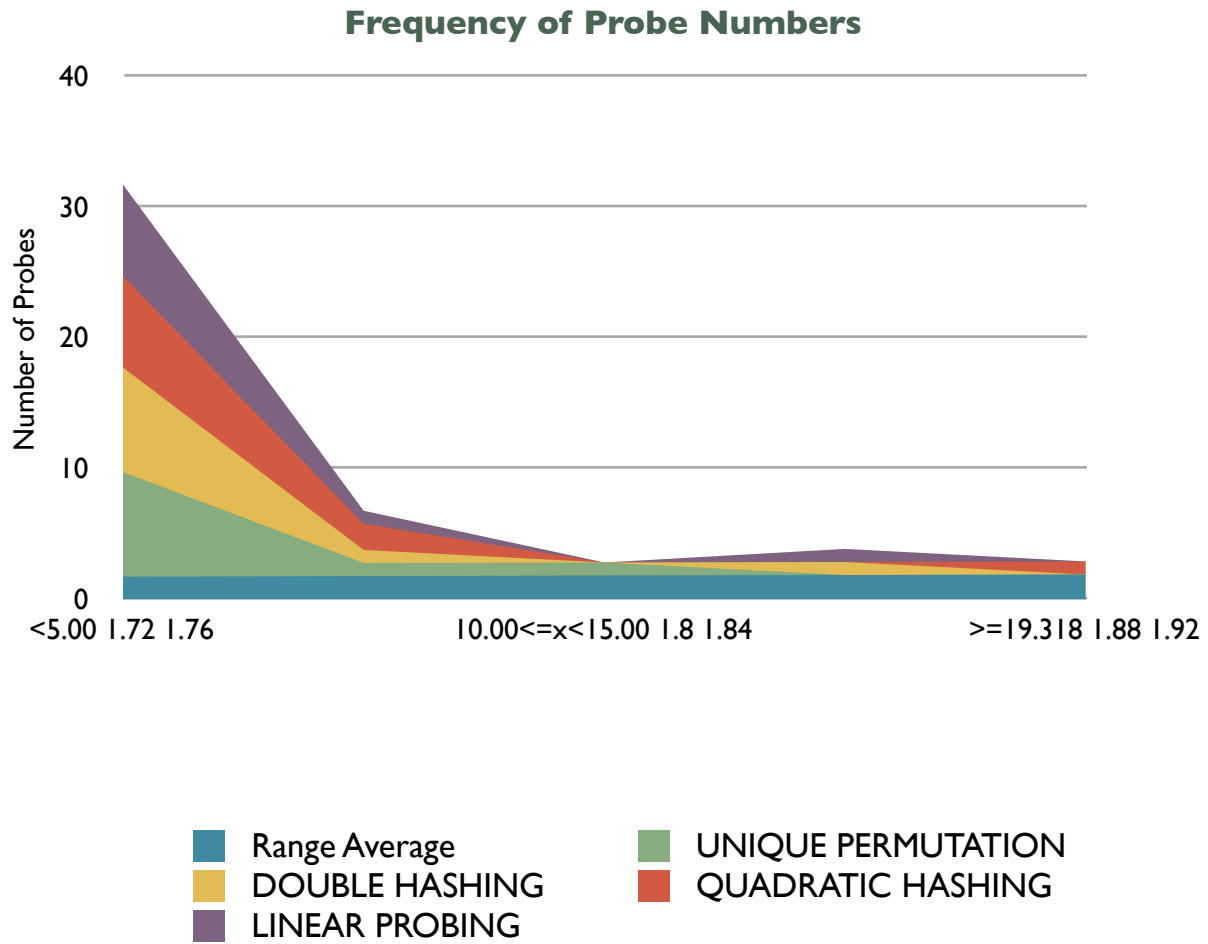


## Calculated Statistics

	<b>UNIQUE PER-MUTATION</b>	<b>DOUBLE HASHING</b>	<b>QUADRATIC HASHING</b>	<b>LINEAR PROBING</b>
<b>Count (ALPHA)</b>	10	10	10	10
<b>Mean</b>	3.147	3.668	4.085	3.528
<b>Median</b>	1.492	1.560	1.654	1.586
<b>Standard deviation</b>	4.410	5.571	6.007	4.887
<b>Variance</b>	19.44512	31.03161	36.08057	23.87900
<b>Alpha</b>	0.05	0.05	0.05	0.05
<b>T-value</b>	2.26	2.26	2.26	2.26
<b>Confidence interval</b>	2.73309	3.45263	3.72293	3.02870
<b>Upper limit</b>	5.87959	7.12073	7.80813	6.55620
<b>Lower limit</b>	0.41341	0.21547	0.36227	0.49880
<b>T-interval</b>	3.15426	3.98469	4.29284	3.49234
<b>Upper limit</b>	6.30076	7.65279	8.37804	7.01984
<b>Lower limit</b>	-0.00776	-0.31659	-0.20764	0.03516

## Frequency Table

<b>Range</b>	<b>UNIQUE PER-MUTATION</b>	<b>DOUBLE HASHING</b>	<b>QUADRATIC HASHING</b>	<b>LINEAR PROBING</b>
<b>&lt;5.00</b>	8	8	7	7
<b>5.00&lt;=x&lt;10.00</b>	1	1	2	1
<b>10.00&lt;=x&lt;15.00</b>	1	0	0	0
<b>15.00&lt;=x&lt;19.318</b>	0	1	0	1
<b>&gt;=19.318</b>	0	0	1	0





## SUMMARY

Overall, unique permutation represents improvement over other hashing functions, particularly double hashing. This is because the former uses permutations of the table size as unique identifiers to insert keys while the latter has a max number of probe sequences that range to the table size exponentiated to 2.

## BIBLIOGRAPHY

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The MIT Press : Cambridge , Massachusetts London , England

Shlomi Dole ; Limo Lahiani ; Yinnon Aviv .”UNIQUE PERMUTATION HASHING “

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